

The Decay $\bar{B} \rightarrow \bar{K}^* \ell^+ \ell^-$ at Low Recoil and its Constraints on New Physics

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Overview

1 FCNCs in Effective Field Theory

2 Hadronic Decays

3 $B \rightarrow K^* \ell^+ \ell^-$ at Low Recoil

4 Global Fit and Constraints on \mathcal{C}_i

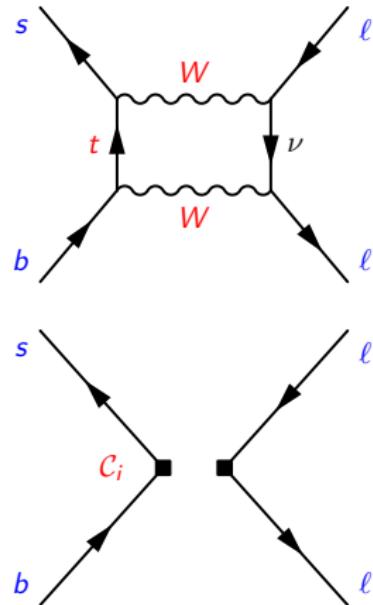
At Parton Level: $b \rightarrow s\ell^+\ell^-$

- Flavor Changing Neutral Current: change of flavor $b \rightarrow s$ in a neutral current
- in the SM W, Z, t propagators occur
- expand amplitudes in $G_F \sim 1/M_W^2$ (OPE)
- find a basis of operators with b, s and two light leptons $\ell = e, \mu$

$$\mathcal{O}_i \equiv [\bar{s}\Gamma_i b] [\bar{\ell}\Gamma'_i \ell]$$

- calculate coefficients of operators

$$\mathcal{C}_i \equiv \mathcal{C}_i(M_W, M_Z, m_t, \dots)$$



Effective Hamiltonian

- use effective Hamiltonian

$$\mathcal{H} = -\frac{4G_F}{\sqrt{2}} \left[\lambda^{(t)} \mathcal{H}^{(t)} + \lambda^{(u)} \mathcal{H}^{(u)} \right], \quad \lambda^{(q)} \equiv V_{qb} V_{qs}^*$$

- make CKM unitary and hierarchy explicit:

$$\begin{aligned}\mathcal{H}^{(t)} &= \sum_{i \neq 1u, 2u} \mathcal{C}_i \mathcal{O}_i \\ \mathcal{H}^{(u)} &= \mathcal{C}_1 \left[\mathcal{O}_{1c} - \mathcal{O}_{1u} \right] + \mathcal{C}_2 \left[\mathcal{O}_{2c} - \mathcal{O}_{2u} \right]\end{aligned}$$

- $\lambda^{(u)}$ small and complex, important when considering CP violating observables

Operators

Semileptonic Operators (SM and χ -flipped)

$$\mathcal{O}_{9(')} = \frac{\alpha_e}{4\pi} [\bar{s}\gamma_\mu P_{L(R)} b] [\bar{\ell}\gamma^\mu \ell] \quad \mathcal{O}_{10(')} = \frac{\alpha_e}{4\pi} [\bar{s}\gamma_\mu P_{L(R)} b] [\bar{q}\gamma^\mu \gamma_5 \ell]$$

Semileptonic Operators (extended)

$$\begin{aligned} \mathcal{O}_S(') &= \frac{\alpha_e}{4\pi} [\bar{s}P_{R(L)} b] [\bar{\ell}\ell] & \mathcal{O}_P(') &= \frac{\alpha_e}{4\pi} [\bar{s}P_{R(L)} b] [\bar{\ell}\gamma_5 \ell] \\ \mathcal{O}_T &= \frac{\alpha_e}{4\pi} [\bar{s}\sigma_{\mu\nu} b] [\bar{\ell}\sigma^{\mu\nu} \ell] & \mathcal{O}_{T5} &= \frac{\alpha_e}{4\pi} [\bar{s}\sigma_{\mu\nu} b] [\bar{\ell}\sigma_{\alpha\beta} \ell] \frac{i\varepsilon_{\mu\nu\alpha\beta}}{2} \end{aligned}$$

Operators (cont.)

Radiative

$$\mathcal{O}_{7(')} = [\bar{s}\sigma_{\mu\nu}P_{R(L)}b]F^{\mu\nu} \quad \mathcal{O}_{8(')} = [\bar{s}\sigma_{\mu\nu}P_{R(L)}b]G^{\mu\nu}$$

Current-Current

Fixed flavors $q = u, c$

$$\mathcal{O}_{1q} = [\bar{s}\gamma_\mu T^a P_L q] [\bar{q}\gamma^\mu T^a P_L b] \quad \mathcal{O}_{2q} = [\bar{s}\gamma_\mu P_L q] [\bar{q}\gamma^\mu P_L b]$$

QCD Penguin

Summation over flavors $q = u, d, s, c, b$

$$\begin{aligned} \mathcal{O}_3 &= [\bar{s}\gamma_\mu P_L b] [\bar{q}\gamma^\mu q] & \mathcal{O}_4 &= [\bar{s}\gamma_\mu T^a P_L b] [\bar{q}\gamma^\mu T^a q] \\ \mathcal{O}_5 &= [\bar{s}\gamma_{\mu\nu\rho} P_L b] [\bar{q}\gamma^{\mu\nu\rho} q] & \mathcal{O}_6 &= [\bar{s}\gamma_{\mu\nu\rho} T^a P_L b] [\bar{q}\gamma^{\mu\nu\rho} T^a q] \end{aligned}$$

$\gamma_{\mu\nu\rho} \equiv \gamma_\mu \gamma_\nu \gamma_\rho$, QED Penguins are usually neglected.

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Exclusive Decays

Possible Hadronic Decays

$$\bar{B}^0 \rightarrow \bar{K}^0 \ell^+ \ell^-$$

$$B^- \rightarrow \bar{K}^- \ell^+ \ell^-$$

$$\bar{B}_s \rightarrow \eta^{(')} \ell^+ \ell^-$$

$$\bar{B}^0 \rightarrow \bar{K}^{*,0} \ell^+ \ell^-$$

$$B^- \rightarrow \bar{K}^{*-} \ell^+ \ell^-$$

$$\bar{B}_s \rightarrow \phi \ell^+ \ell^-$$

... and higher resonances

Naive Factorization

assumes

$$\langle \ell^+ \ell^- V | \mathcal{H} | B \rangle = \langle \ell^+ \ell^- | J^{\text{e.m.}} | 0 \rangle \times \langle V | J^{\text{had.}} | B \rangle$$

broken in principle by QCD: $b \rightarrow s \bar{q} q (\rightarrow \ell^+ \ell^-)$, but at which order?

$B \rightarrow V$ Form Factors

Hadronic Matrix Elements

$$\langle V(k, \eta) | \bar{s} \Gamma b | B(p) \rangle$$

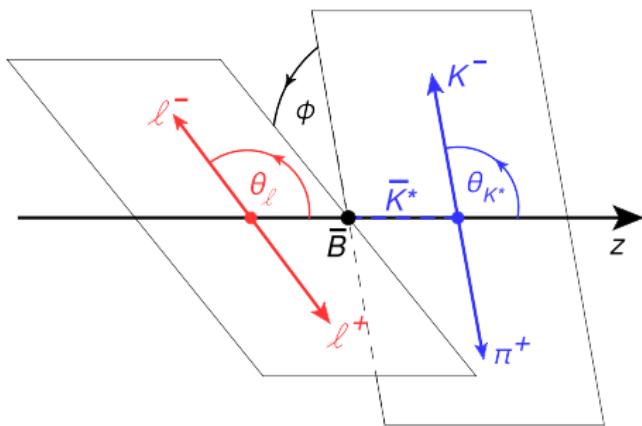
- non-perturbative quantities
- sources: Lattice QCD, Light Cone Sum Rules (LCSR)
- currently largest source of theory uncertainties

Form Factors

- 7 scalar functions, dependent on $q^2 = (p - k)^2$
- parametrize hadronic matrix elements
- make use of transformation properties
- Example

$$\langle V(k, \eta) | \bar{s} \gamma^\mu b | B(p) \rangle = \frac{2V(q^2)}{M_B + M_V} \eta_\nu^* p_\rho k_\sigma \varepsilon^{\mu\nu\rho\sigma}$$

Kinematics of $\bar{B} \rightarrow \bar{K}^*(\rightarrow \bar{K}\pi)\ell^+\ell^-$



Kinematic Variables

$$\begin{aligned} 4m_\ell^2 &\leq q^2 \leq (M_B - M_V)^2 \\ -1 &\leq \cos \theta_\ell \leq 1 \\ -1 &\leq \cos \theta_{K^*} \leq 1 \\ 0 &\leq \phi \leq 2\pi \end{aligned}$$

On-shell and S-Wave

- assumes on-shell decay of K^* , currently hot topic
- for high precision consider width of K^* , and $J = 0$ (S-wave)
 $K\pi$ -final-state from K_0^* and non-resonant background

Angular Distribution

[Krüger/Matias '05]

Calculate fully differential decay rate for pure P wave state

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_{K^*} d\phi} = \frac{3}{8\pi} J(q^2, \cos\theta_\ell, \cos\theta_{K^*}, \phi)$$

$$\begin{aligned}
 J(q^2, \theta_\ell, \theta_{K^*}, \phi) = & J_{1s} \sin^2 \theta_{K^*} + J_{1c} \cos^2 \theta_{K^*} \\
 & + (J_{2s} \sin^2 \theta_{K^*} + J_{2c} \cos^2 \theta_{K^*}) \cos 2\theta_\ell \\
 & + J_3 \sin^2 \theta_{K^*} \sin^2 \theta_\ell \cos 2\phi \\
 & + (J_4 \sin 2\theta_{K^*}) \sin 2\theta_\ell \cos \phi \\
 & + (J_5 \sin 2\theta_{K^*}) \sin \theta_\ell \cos \phi \\
 & + (J_{6s} \sin^2 \theta_{K^*} + J_{6c} \cos^2 \theta_{K^*}) \cos \theta_\ell \\
 & + (J_7 \sin 2\theta_{K^*}) \sin \theta_\ell \sin \phi \\
 & + (J_8 \sin 2\theta_{K^*}) \sin 2\theta_\ell \sin \phi \\
 & + J_9 \sin^2 \theta_{K^*} \sin^2 \theta_\ell \sin 2\phi,
 \end{aligned}$$

Angular Distribution

[Krüger/Matias '05, Blake/Egede/Shires '12]

Calculate fully differential decay rate for mixed P and S wave state

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_{K^*} d\phi} = \frac{3}{8\pi} J(q^2, \cos\theta_\ell, \cos\theta_{K^*}, \phi)$$

$$\begin{aligned}
 J(q^2, \theta_\ell, \theta_{K^*}, \phi) = & J_{1s} \sin^2 \theta_{K^*} + J_{1c} \cos^2 \theta_{K^*} + J_{1i} \cos \theta_{K^*} \\
 & + (J_{2s} \sin^2 \theta_{K^*} + J_{2c} \cos^2 \theta_{K^*} + J_{2i} \cos \theta_{K^*}) \cos 2\theta_\ell \\
 & + J_3 \sin^2 \theta_{K^*} \sin^2 \theta_\ell \cos 2\phi \\
 & + (J_4 \sin 2\theta_{K^*} + J_{4i} \cos \theta_{K^*}) \sin 2\theta_\ell \cos \phi \\
 & + (J_5 \sin 2\theta_{K^*} + J_{5i} \cos \theta_{K^*}) \sin \theta_\ell \cos \phi \\
 & + (J_{6s} \sin^2 \theta_{K^*} + J_{6c} \cos^2 \theta_{K^*}) \cos \theta_\ell \\
 & + (J_7 \sin 2\theta_{K^*} + J_{7i} \cos \theta_{K^*}) \sin \theta_\ell \sin \phi \\
 & + (J_8 \sin 2\theta_{K^*} + J_{8i} \cos \theta_{K^*}) \sin 2\theta_\ell \sin \phi \\
 & + J_9 \sin^2 \theta_{K^*} \sin^2 \theta_\ell \sin 2\phi,
 \end{aligned}$$

Angular Observables

Helicity Decomposition

$$g_{\mu\nu} = \sum_{n,m} g_{nm} \varepsilon_\mu^\dagger(n) \varepsilon_\nu(m) \quad n, m = t, 0, +, -$$

$$-g_{\mu\nu} + \frac{k_\mu k_\nu}{k^2} = \sum_{n,m} \delta_{mn} \eta_\mu^\dagger(n) \eta_\nu(m) \quad n, m = 0, +, -$$

Transversity Amplitudes (SM)

- first use helicity amplitudes

$$H_{ab} = \eta_\mu^\dagger(a) \mathcal{M}^{\mu\nu} \varepsilon_\nu^\dagger(b)$$

- four non-vanishing amp. $H_{\pm\pm}, H_{00}, H_{0t}$
- transversity basis: $A_{\perp,\parallel} = (H_{++} \mp H_{--})/\sqrt{2}$, $A_0 = H_0$, $A_t = H_{0t}$
- extended operator basis → more amplitudes

Angular Observables (cont')

Transversity Amplitudes (extended basis) [Bobeth/Hiller/DvD '12]

- extended operator basis → more amplitudes
- $S(')$: A_S , $P(')$: absorbed by A_t [Altmannshofer et al. '08]
- $T(5)$: 6 new amps A_{ab} (ab) = $(0t), (\parallel \perp), (0\perp), (t\perp), (0\parallel), (t\parallel)$

$$H_{abc} = \eta_\mu^\dagger(a) \mathcal{M}^{\mu\nu\rho} \varepsilon_\nu^\dagger(b) \varepsilon_\rho^\dagger(c)$$

$$A_{ab} = \text{linear com. of } (H_{xyz}) \quad a, b = t, 0, \parallel, \perp \quad x, y, z = t, 0, +, -$$

Angular Observables

- J_i functionals of A_S, A_a, A_{ab} , $a, b = t, 0, \parallel, \perp$
- example

$$J_3(q^2) = \frac{3\beta_\ell}{4} \left[|A_\perp|^2 - |A_\parallel|^2 + 16(|A_{t\parallel}|^2 + |A_{0\parallel}|^2 - |A_{t\perp}|^2 - |A_{0\perp}|^2) \right]$$

Further Observables

CP Conserving

- decay width

$$\frac{d\Gamma}{dq^2} = \frac{6J_{1s} + 3J_{1c} - 2J_{2s} + J_{2c}}{3}$$

- forward-backward asymmetry

$$A_{FB}(q^2) = \frac{2J_{6s} + J_{6c}}{2d\Gamma/dq^2}$$

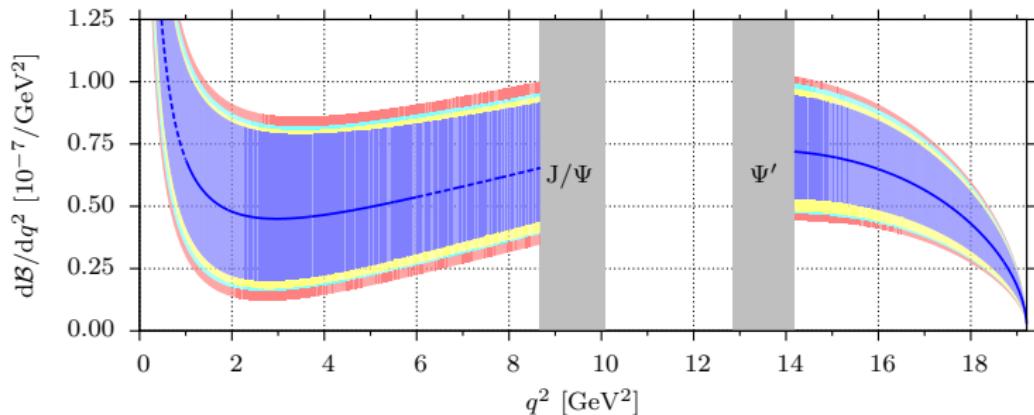
- longitudinal/transversal polarization

$$F_L = \frac{3J_{1c} - J_{2c}}{3d\Gamma/dq^2} \quad F_T = \frac{3J_{1s} - J_{2s}}{6d\Gamma/dq^2} \quad F_L + F_T = 1$$

Further

- CP asymmetries of the angular observables
- isospin asymmetries of the angular observables

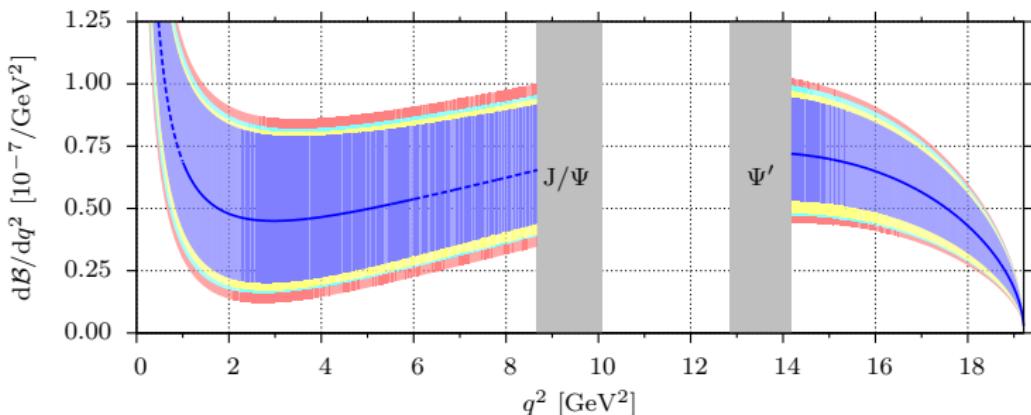
q^2 Spectrum of the Branching Ratio $\mathcal{B} = \tau_B \Gamma$



$\bar{q}q$ Pollution

- 4-quark operators like $\mathcal{O}_{1c,2c}$ induce $b \rightarrow s\bar{c}c(\rightarrow \ell^+\ell^-)$ via loops
- hadronically $B \rightarrow K^* J/\psi(\rightarrow \ell^+\ell^-)$ or higher charmonia
- experiment: cut narrow resonances $J\psi \equiv \psi(1S)$ and $\psi' = \psi(2S)$
- theory: handle non-resonant quark loops/broad resonances $> 2S$

q^2 Spectrum of the Branching Ratio $\mathcal{B} = \tau_B \Gamma$



Large Recoil $E_{K^*} \sim m_b$ QCDF, SCET

- expand in $1/m_b$, $1/E_{K^*}$, α_s
- symmetry: $7 \rightarrow 2$ form factors

[Beneke/Feldmann/Seidel '01 & '04]

[Egede et al. '08 & '10]

Low Recoil $q^2 \sim m_b^2$ OPE, HQET

- expand in $1/m_b$, $1/\sqrt{q^2}$, α_s
- symmetry: $7 \rightarrow 4$ form factors

[Grinstein/Pirjol '04], [Beylich/Buchalla/Feldmann '11]

[Bobeth/Hiller/DvD '10 & '11]

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Improved Isgur-Wise Relations

Operator Identity

$$i\partial^\nu [\bar{s}i\sigma_{\mu\nu} b] = -(m_b + m_s)[\bar{s}\gamma_\mu b] + i\partial_\mu[\bar{s}b] - 2[\bar{s}i\overleftarrow{D}_\mu b]$$

Tensor Form Factors

- apply op.id. to hadronic matrix elements
- left-hand side

$$\langle V(k, \eta) | \bar{s}\sigma_{\mu\nu} q^\nu b | B(p) \rangle \sim T_1, T_2, T_3$$

- right-hand side

$$\langle V(k, \eta) | \bar{s}\gamma_\mu(\gamma_5) b | B(p) \rangle \sim V(A_0, A_1, A_2)$$

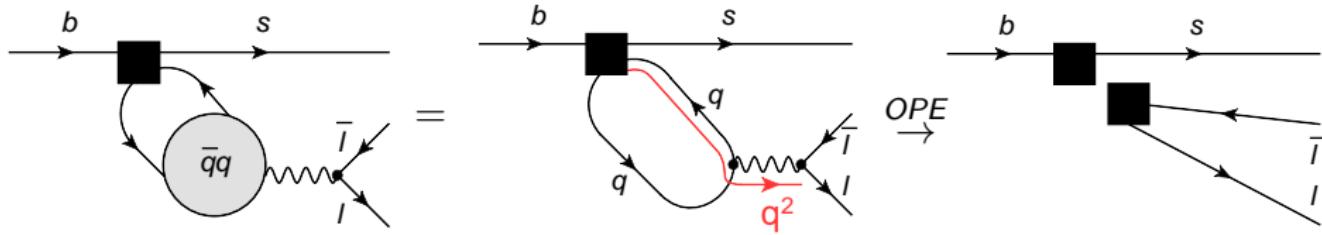
- read off improved Isgur-Wise relations ($\kappa(m_b) = 1 + O(\alpha_s^2)$)

$$T_1 = \kappa V \qquad \qquad T_2 = \kappa A_1 \qquad \qquad T_3 = \kappa \frac{M_B^2}{q^2} A_2$$

Local OPE

[Grinstein/Pirjol '04, Beylich/Buchalla/Feldmann '11]

$$i \int d^4x e^{iqx} \langle \bar{K}^* | T\{\mathcal{O}_i(0), j_\mu^{\text{e.m.}}(x)\} | \bar{B} \rangle = \sum_{j,k} \mathcal{C}_{i,j,k}(q^2/m_b^2, \mu) \langle \mathcal{O}_j^{(k)} \rangle_\mu$$



Operators

$k = 3$ form factors, α_s corrections known, absorbed into effective Wilson coefficients $\mathcal{C}_{7,9} \rightarrow \mathcal{C}_{7,9}^{\text{eff}}$

$k = 4$ absent

$k = 5$ $\Lambda^2/m_b^2 \sim 2\%$ corrections, first new had. matrix elements explicitly: < 1% for $q^2 = 15 \text{ GeV}^2$ [Beylich/Buchalla/Feldmann]

$k = 6$ first isospin breaking correction, Λ^3/m_b^3 suppressed

Low Recoil Framework Put Together

SM Basis

- TA factorize to $O(\alpha_s \Lambda / m_b, \mathcal{C}_7 \Lambda / (\mathcal{C}_9 m_b))$ [Grinstein/Pirjol '04, Bobeth/Hiller/DvD '10]

$$A_{0,\perp,\parallel}^{L(R)} = NC^{L(R)} f_{0,\perp,\parallel}$$

- f_i : helicity form factors [Bharucha/Feldmann/Wick '10]
- in spin-averaged decays: only two short-distance coefficients

$$2\rho_1 = |C^L|^2 + |C^R|^2 \quad 4\rho_2 = |C^L|^2 - |C^R|^2$$

- all observables are either [Bobeth/Hiller/DvD '10]
 - ρ_1 dependent
 - ρ_2/ρ_1 dependent
 - free of short-distance coefficients

$$\Gamma \sim \rho_1 \quad A_{\text{FB}} \sim \frac{\rho_2}{\rho_1} \quad F_L : \text{SD free}$$

Optimized Observables

- no form factor dependence by design

$$H_T^{(1)} \equiv \frac{\sqrt{2} J_4}{\sqrt{-J_{2c}(2J_{2s} - J_3)}} = \text{sgn}(f_0)$$

$$H_T^{(2)} \equiv \frac{\beta_\ell J_5}{\sqrt{-J_{2c}(2J_{2s} + J_3)}} = 2 \frac{\rho_2}{\rho_1}$$

$$H_T^{(3)} \equiv \frac{\beta_\ell J_{6s}}{2\sqrt{(2J_{2s}^2 - J_3^2)}} = 2 \frac{\rho_2}{\rho_1}$$

- $H_T^{(1)}$ probes the OPE
- $H_T^{(2,3)}$ sensitive to $\mathcal{C}_9/\mathcal{C}_{10}$

Beyond the SM

[Bobeth/Hiller/DvD '12]

Amplitudes (extended basis)

- all TA factorize for $\ell = e, \mu$ and in absence of scalar operators

$$A_{0,\parallel}^{L(R)} = -NC_-^{L(R)} f_{0,\parallel} \quad A_\perp^{L(R)} = +NC_+^{L(R)} f_\perp$$

$$A_{0(t)\perp} \sim C_{T(5)} f_\perp \quad A_{0(t)\parallel} \sim C_{T(5)} f_\parallel \quad A_{\parallel\perp(t0)} \sim C_{T(5)} f_0$$

$$\rho_1 \rightarrow \rho_1^\pm = \frac{1}{2}(|C_\pm^R|^2 + |C_\pm^L|^2) \quad \rho_2 \rightarrow \frac{1}{4}(C_+^R C_-^{R*} - C_-^L C_+^{L*})$$

More Optimized Observables

- existing observables

$$H_T^{(2)} = H_T^{(3)} = 2 \operatorname{Re}(\rho_2) / \sqrt{\rho_1^- \rho_1^+}$$

- new observables

$$H_T^{(4)} \equiv \frac{\sqrt{2} J_8}{\sqrt{-J_{2c}(2J_{2s} + J_3)}} = 2 \operatorname{Im}(\rho_2) / \sqrt{\rho_1^- \rho_1^+}$$

$$H_T^{(5)} \equiv \frac{-J_9}{\sqrt{(2J_{2s})^2 - J_3^2}} = 2 \operatorname{Im}(\rho_2) / \sqrt{\rho_1^- \rho_1^+}$$

Beyond the SM (cont')

[Bobeth/Hiller/DvD '12]

Relations at Low Recoil

| Scenario | $ H_T^{(1)} = 1$ | $H_T^{(2)} = H_T^{(3)}$ | $H_T^{(4)} = H_T^{(5)}$ | $J_7 = 0$ | $J_{8,9} = 0$ |
|--------------------|----------------------------------|-----------------------------------------------------------------------------|-----------------------------------------------------|-----------------------------------------------------------------------------|-----------------------------------|
| SM | ✓ | ✓ | (✓) | ✓ | ✓ |
| $SM \otimes S, P$ | ✓ | $\frac{m_\ell}{Q} \operatorname{Re}(\mathcal{C}_-^{\text{L,R}} \Delta_S^*)$ | (✓) | $\frac{m_\ell}{Q} \operatorname{Im}(\mathcal{C}_+^{\text{L,R}} \Delta_S^*)$ | ✓ |
| $SM \otimes T, T5$ | $\frac{M_{K^*}^2}{Q^2} \rho_1^T$ | $\frac{m_\ell}{Q} \operatorname{Re}(\rho_2^T)$ | $\frac{M_{K^*}}{Q} \operatorname{Im}(\rho_2^T)$ | $\frac{m_\ell}{Q} \operatorname{Im}(\mathcal{C}_i \mathcal{C}_{T5}^*)$ | $\operatorname{Im}(\rho_2^T)$ |
| $SM \otimes SM'$ | ✓ | ✓ | ✓ | ✓ | $\operatorname{Im}(\rho_2)$ |
| all | $\frac{M_{K^*}^2}{Q^2} \rho_1^T$ | $\operatorname{Re}(\mathcal{C}_{T5} \Delta_S^*)$ | $\frac{M_{K^*}}{Q} \operatorname{Im}(\rho_2^{(T)})$ | $\operatorname{Im}(\mathcal{C}_{T5} \Delta_S^*)$ | $\operatorname{Im}(\rho_2^{(T)})$ |

$$\rho_1^T \sim |\mathcal{C}_T|^2 + |\mathcal{C}_{T5}|^2 \quad \rho_2^T \sim \operatorname{Re}(\mathcal{C}_T \mathcal{C}_{T5})$$

$$\Delta_S = \mathcal{C}_S - \mathcal{C}_{S'} \quad Q = m_b, \sqrt{q^2}$$

Factorization

| Scenario | $H_T^{(1)}$ | $H_T^{(2)}$ | $H_T^{(3)}$ | $H_T^{(4)}$ | $H_T^{(5)}$ |
|--------------------|-------------|-------------|-------------|-------------|-------------|
| SM | ✓ | ✓ | ✓ | — | — |
| $SM \otimes S, P$ | ✓ | A_0 | ✓ | — | — |
| $SM \otimes T, T5$ | ✓ | ✓ | ✓ | ✓ | ✓ |
| $SM \otimes SM'$ | ✓ | ✓ | ✓ | ✓ | ✓ |
| all | ✓ | A_0 | ✓ | ✓ | ✓ |

—: vanishes in that scenario

✓: form factor free up to m_ℓ/Q

A_0 : factorization broken by terms $\propto A_0$

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Global Fit

[Beaujean/Bobeth/DvD/Wacker '12]

Method

[see also Dissertation Beaujean '12]

Black Box!

- explore with Markov Chain Monte Carlo
- group samples with Hierarchical Clustering
- sample efficiently with Population Monte Carlo [Kilbinger et al. '09]

see also talk on sampling in high-dimensional spaces (informal seminar)

Implementation

- EOS: C++, open source GPLv2
- programs for evaluation of observables, uncertainties, fits
- available via
<http://project.het.physik.tu-dortmund.de/eos/source>

Inputs

Exclusive Decays

- $\bar{B} \rightarrow \bar{K}^* \ell^+ \ell^-$, large & low recoil
 observables: $\mathcal{B} = \tau_B \Gamma$, A_{FB} , F_L , $A_T^{(2)}$, S_3
 experiments: BaBar, Belle, CDF, LHCb, several bins each
- $\bar{B} \rightarrow \bar{K} \ell^+ \ell^-$, large & low recoil
 observables: \mathcal{B} several bins each experiments: BaBar, Belle, CDF
 (LHCb is now available!)
- $B_s \rightarrow \mu^+ \mu^-$
 observable: $\mathcal{B}(t=0)$ (see [de Bruyn et al. '12]) experiment: combination ATLAS+CMS+LHCb (best upper bound to date)
- $B^0 \rightarrow K^{*0} (\rightarrow K_S \pi^0) \gamma$
 observable: \mathcal{B} , $S_{K^*\gamma}$, $C_{K^*\gamma}$
 experiment: CLEO, BaBar, Belle

Parameters

Interest: $\mathcal{C}_{7,9,10}$

3 real valued parameters, flat prior

Nuisance: Subleading Contributions

one factor per amplitude (6) per kinematic region (12 altogether), gaussian prior

Nuisance: Hadronic Parameters

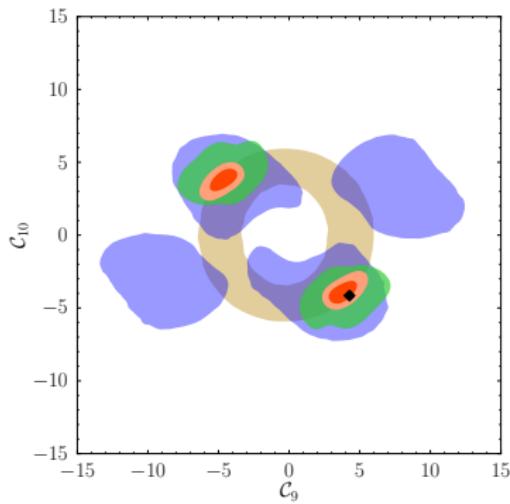
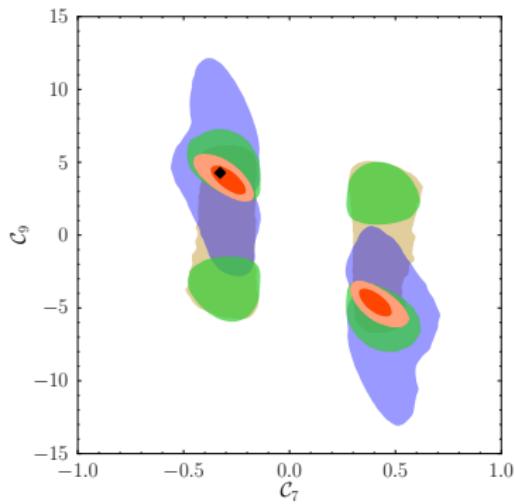
- $B \rightarrow K^*$ form factors (BZ2004: V, A_1, A_2), gaussian prior
- $B \rightarrow K$ form factors (KMPW2010: f_+), gaussian prior
- decay constant f_{B_s} , gaussian prior

Nuisance: CKM Wolfenstein Parameters

input from UTfit, tree level results, **uncorrelated** gaussian prior

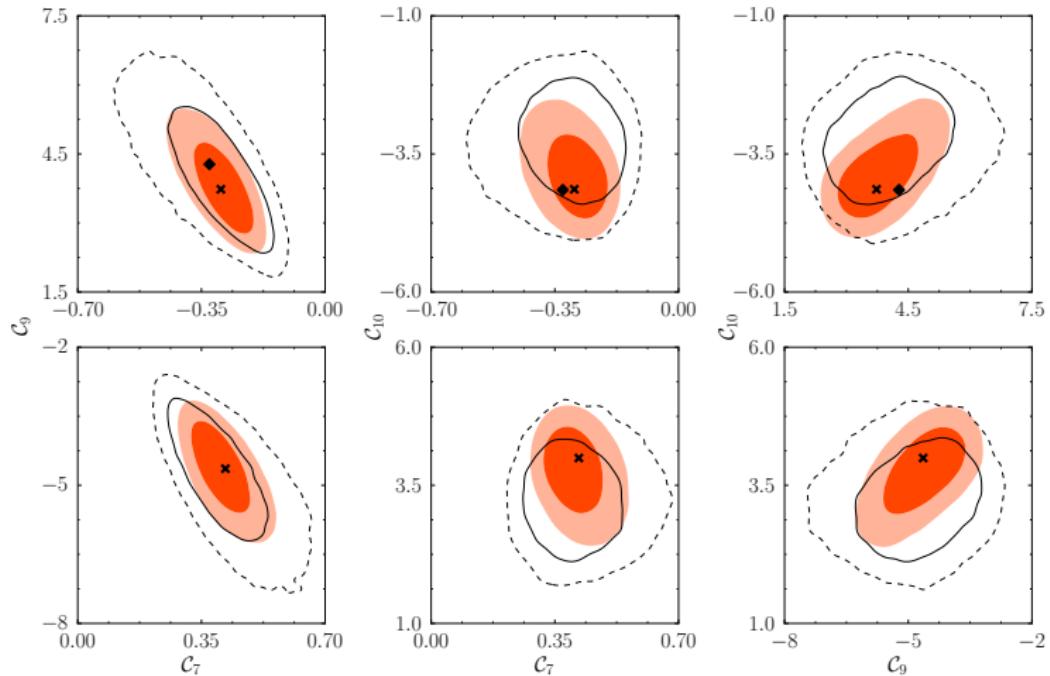
Results for Parameters of Interest

95% credibility regions



all regions include $B \rightarrow K^*\gamma$ inputs
 brown incl. $B \rightarrow K\ell^+\ell^-$ (high + low)
 blue incl. $B \rightarrow K^*\ell^+\ell^-$ (low)
 light red all data + $B_s \rightarrow \mu^+\mu^-$
 green incl. $B \rightarrow K^*\ell^+\ell^-$ (high)
 dark red same at 65%

Results for Different Sets of Priors



color: normal priors (dark: 68%, light: 95%)

lines: wide priors (solid: 68%, dashed: 95%)

diamond: SM, cross: MAP

Results for Parameters of Interest

| | \mathcal{C}_7 | \mathcal{C}_9 | \mathcal{C}_{10} |
|-----|------------------------------------|--------------------------------|--------------------------------|
| 68% | $[-0.34, -0.23] \cup [0.35, 0.45]$ | $[-5.2, -4.0] \cup [3.1, 4.4]$ | $[-4.4, -3.4] \cup [3.3, 4.3]$ |
| 95% | $[-0.41, -0.19] \cup [0.31, 0.52]$ | $[-5.9, -3.5] \cup [2.6, 5.2]$ | $[-4.8, -2.8] \cup [2.7, 4.7]$ |
| max | $-0.28 \cup 0.40$ | $-4.56 \cup 3.64$ | $-3.92 \cup 3.86$ |
| 68% | $[-0.39, -0.19] \cup [0.30, 0.48]$ | $[-5.6, -3.8] \cup [2.9, 5.1]$ | $[-4.0, -2.5] \cup [2.6, 3.9]$ |
| 95% | $[-0.53, -0.13] \cup [0.24, 0.61]$ | $[-6.7, -3.1] \cup [2.2, 6.2]$ | $[-4.7, -1.9] \cup [2.0, 4.6]$ |
| max | $-0.30 \cup 0.38$ | $-4.64 \cup 3.84$ | $-3.24 \cup 3.30$ |

upper: normal priors

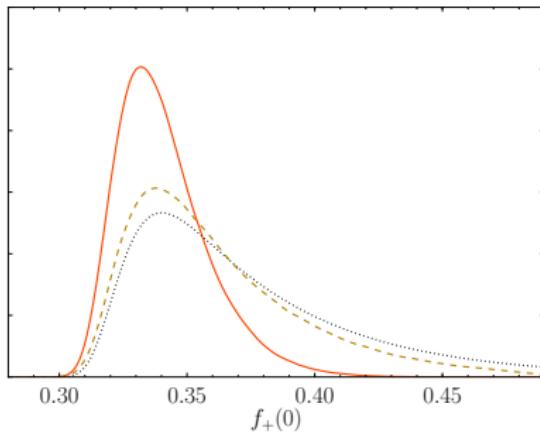
lower: wide priors

Very good agreement with the SM!

From 59 exper. inputs, only one pull $> 2\sigma$! ($\mathcal{B}[B \rightarrow K^* \ell^+ \ell^-]_{>16}$ Belle)

Results for Nuisance Parameters

$B \rightarrow K\ell^+\ell^-$



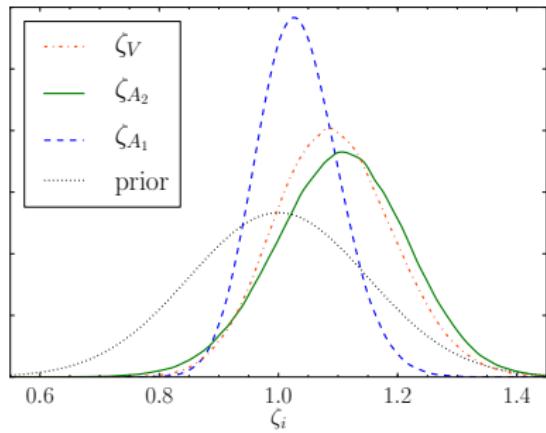
$f_+(q^2)$ form factor, two parameters,
 z parametrisation

dotted: prior

dashed: only $B \rightarrow K\ell^+\ell^-$ data

solid: all data

$B \rightarrow K^*\ell^+\ell^-$



$V(q^2) \rightarrow \zeta_V V(q^2)$, etc.
 considerable shifts ($\sim 10\%$) in V and A_2 !

Conclusion

Low Recoil

- systematic framework, rich phenomenology
- large number of stable relations between $H_T^{(i)}$
- framework/OPE can be probed
- LHCb providing more data, looking forward to Super Flavor Factories

Global Fit

- best fit close to SM, within 1σ , SM wins over model-independent fit
- extract information about form factors, subleading contributions
- slight tension between $B \rightarrow K$ and $B \rightarrow K^*$ form factors $\sim 10\%$
- inclusive decays $B \rightarrow X_s \ell^+ \ell^-$, $B \rightarrow X_s \gamma$ w.i.p.

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CP Asymmetries at Low Recoil

Optimized CP Asymmetries

$$a_{\text{CP}}^{(1)} = A_{\text{CP}} = \frac{\rho_1 - \bar{\rho}_1}{\rho_1 + \bar{\rho}_1}$$

$$a_{\text{CP}}^{(2)} = A_{\text{CP,FB}} = \frac{\frac{\rho_2}{\rho_1} - \frac{\bar{\rho}_2}{\bar{\rho}_1}}{\frac{\rho_2}{\rho_1} + \frac{\bar{\rho}_2}{\bar{\rho}_1}}$$

$$a_{\text{CP}}^{(3)} = \frac{\text{Re}(\rho_2 - \bar{\rho}_2)}{\rho_1 + \bar{\rho}_1} \sim H_T^{(2,3)}$$

$$a_{\text{CP}}^{(4)} = \frac{\text{Im}(\rho_2 - \bar{\rho}_2)}{\rho_1 + \bar{\rho}_1} \sim H_T^{(4,5)}$$

driven by

$$\text{Im}(Y) = \text{Im} \left(Y_9 + \kappa \frac{2m_b M_B}{q^2} Y_7 \right)$$

compare

$$\mathcal{C}_{7,9}^{\text{eff}} = \mathcal{C}_{7,9} + Y_{7,9}$$

γ at Low Recoil

